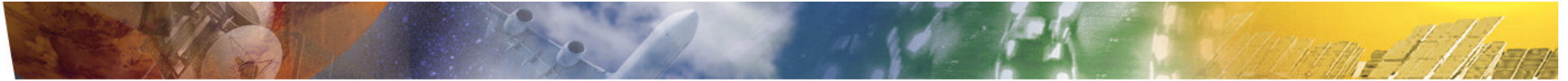


# **Forest Parameter Estimation in Tropical Forests by means of Pol-InSAR: Evaluation of the INDREX II Campaign**

**Florian Kugler, K.P. Papathanassiou & Irena Hajnsek**



# Agenda

*Theory Random Volume over Ground Model*

*Sungai Wain Test Site*

*Ground Truth*

*Topography*

*Inversion Results L Band and P Band*

*Mawas Test Site*

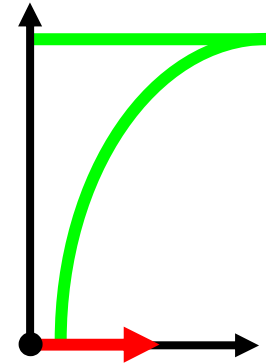
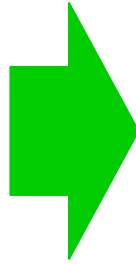
*Ground Truth*

*Inversion Results X Band*

*Summary*



# Random Volume over Ground (RVoG) Scattering Model



*Interferometric Coherence:*

$$\tilde{\gamma}(\vec{w}) = \exp(i\varphi_0) \frac{\tilde{\gamma}_V + m(\vec{w})}{1 + m(\vec{w})}$$

*Volume Coherence:*

$$\tilde{\gamma}_V = \frac{I}{I_0}$$

$$\left\{ \begin{array}{l} I = \int_0^{h_V} \exp(ik_z z') \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz' \\ I_0 = \int_0^{h_V} \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz' \end{array} \right.$$

*G/V Ratio:*  $m(\vec{w}) = \frac{m_G(\vec{w})}{m_V(\vec{w})I_0}$

*Vertical Wavenumber:*  $\kappa_z = \frac{\kappa\Delta\theta}{\sin(\theta_0)}$

**4 Parameters:**

*Volume height*  $h_V$

*Extinction*  $\sigma$

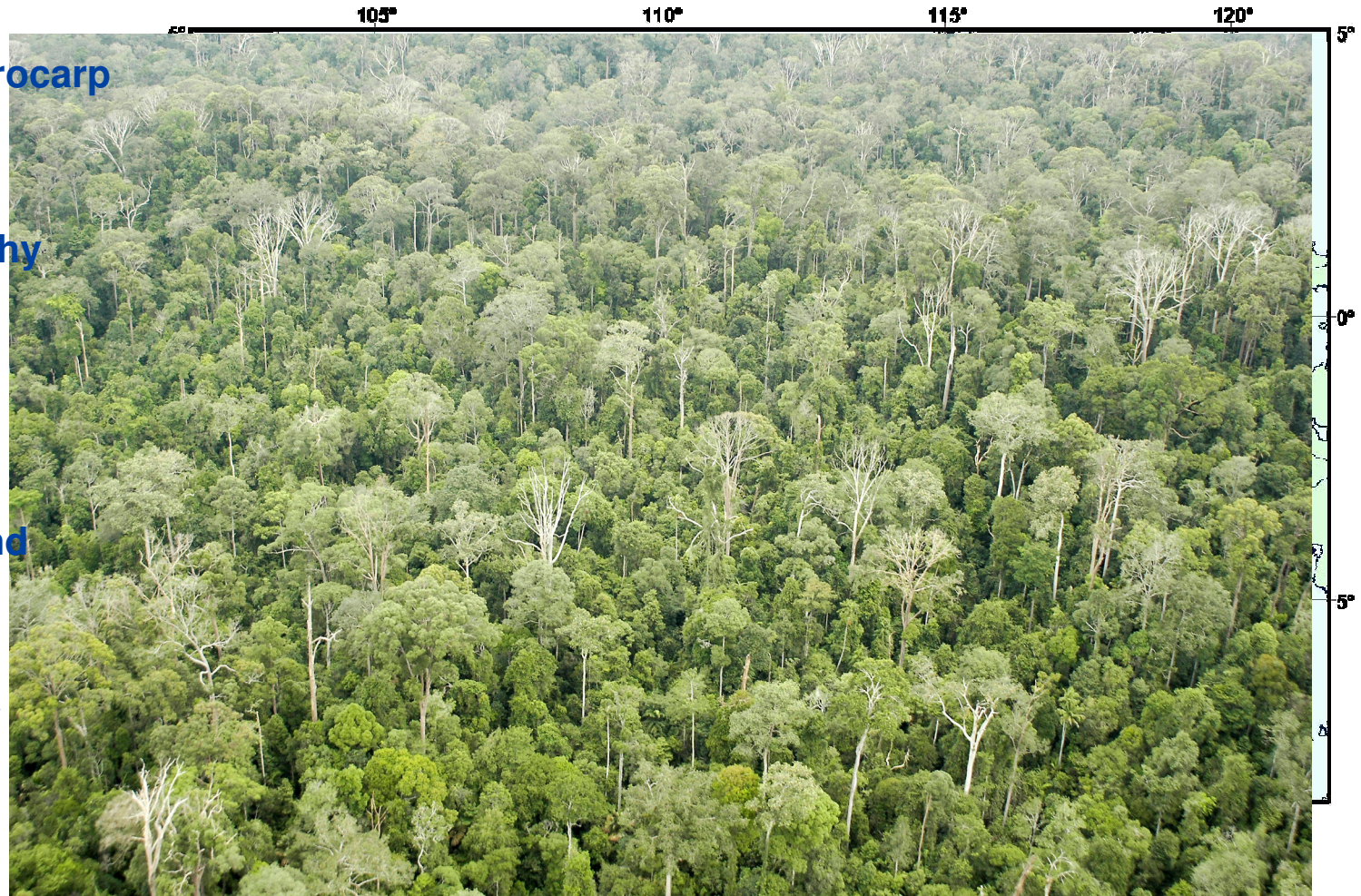
*Topography*  $\varphi_0$

*G/V Ratio*  $m(\vec{w})$



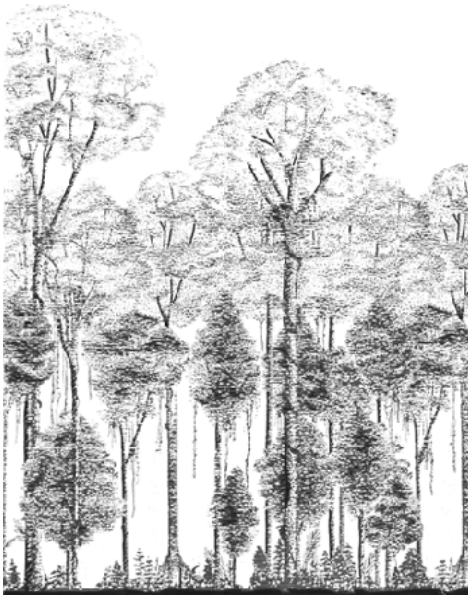
# Test Site: Sungai Wain

- Lowland Dipterocarp Forest
- Hilly Topography
- Forest Height: 10m – 50m
- Biomass around 100 - 400t/ha
- Closed canopy
- Dense





# Reference Height Sungai Wain

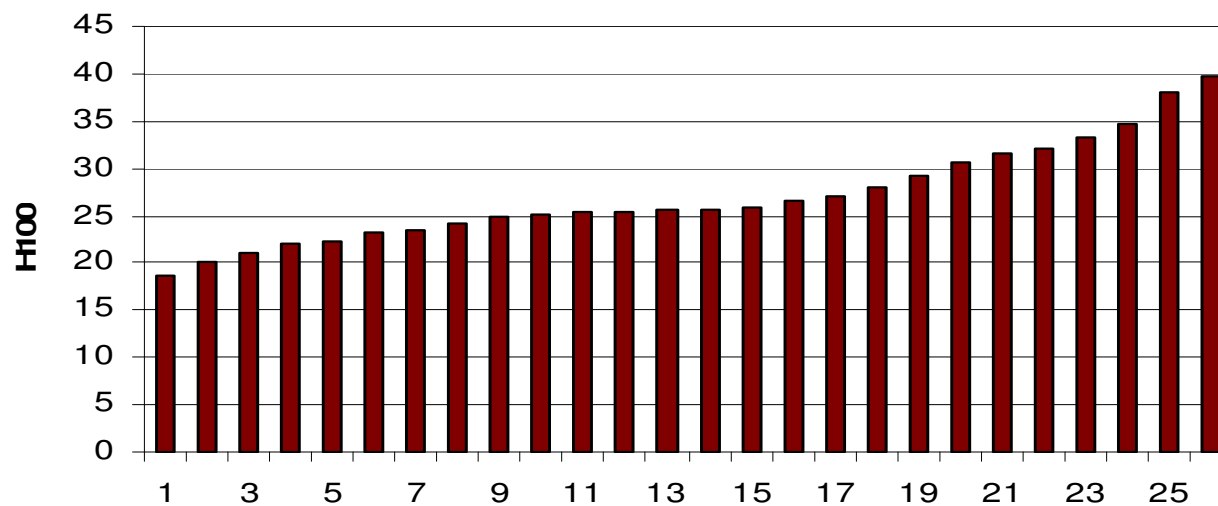
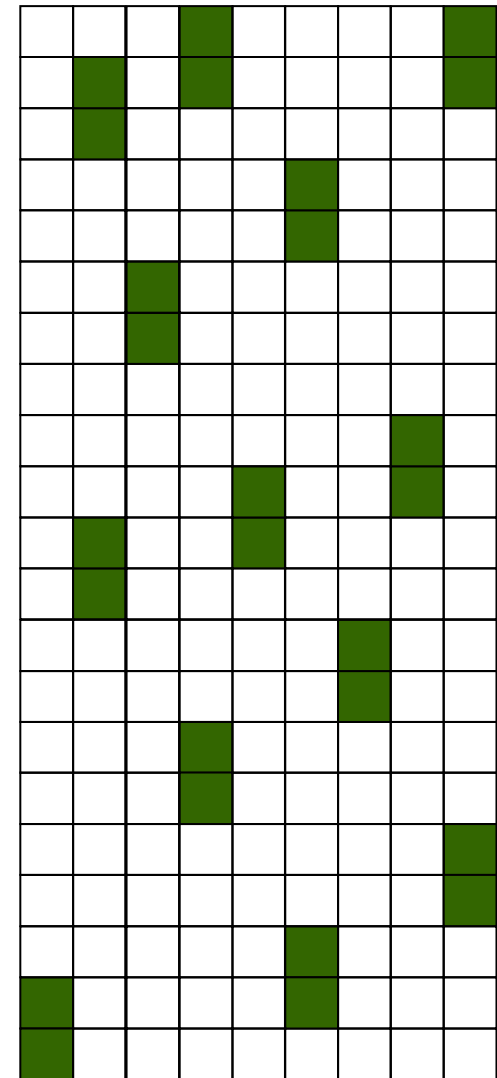


Plot design: 216m x 672m

5.4 ha plot

Suplots: 24m x 32m

Top Height H100 for each Subplot  
Mean height of subplots: 27m

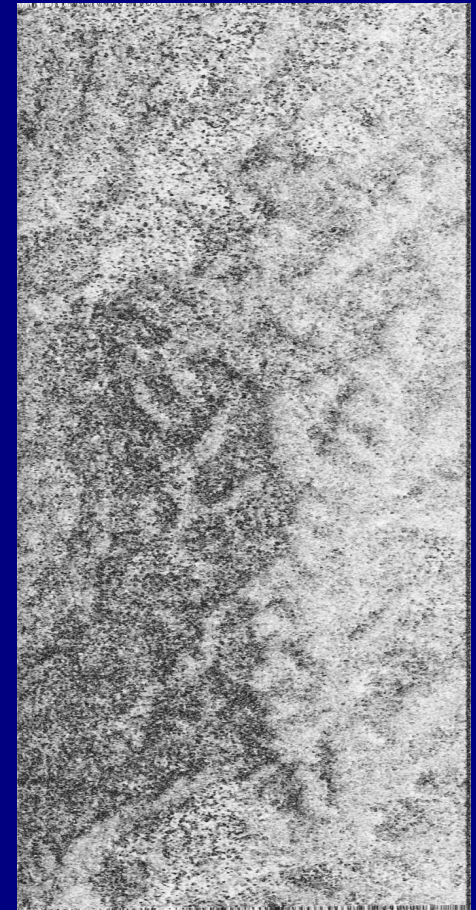
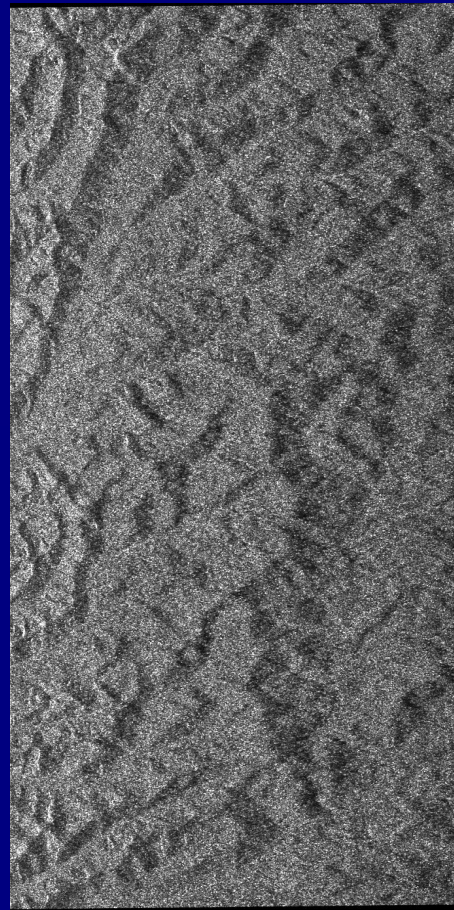
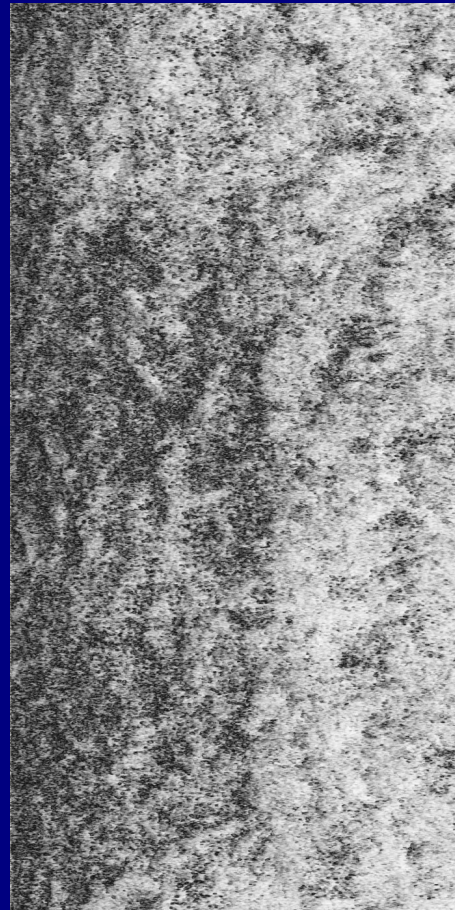
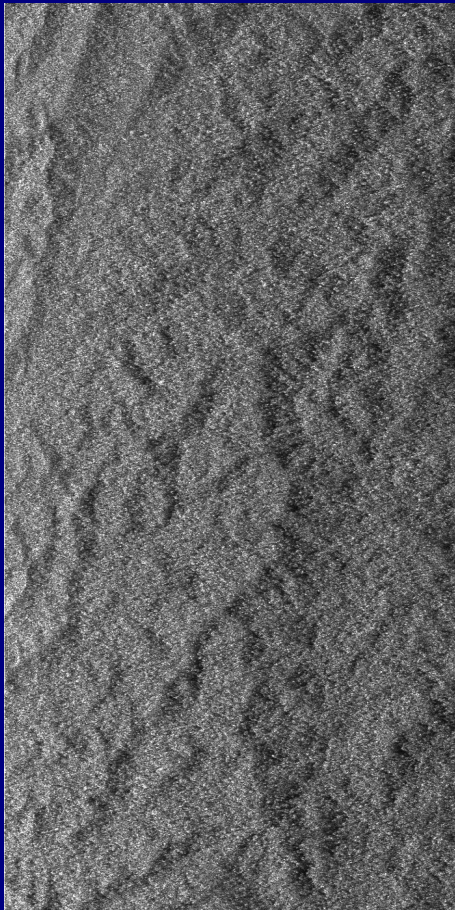




# Radar Data Sungai Wain

**L Band**

**P Band**



**Amplitude**

**Coherence**

**Amplitude**

**Coherence**



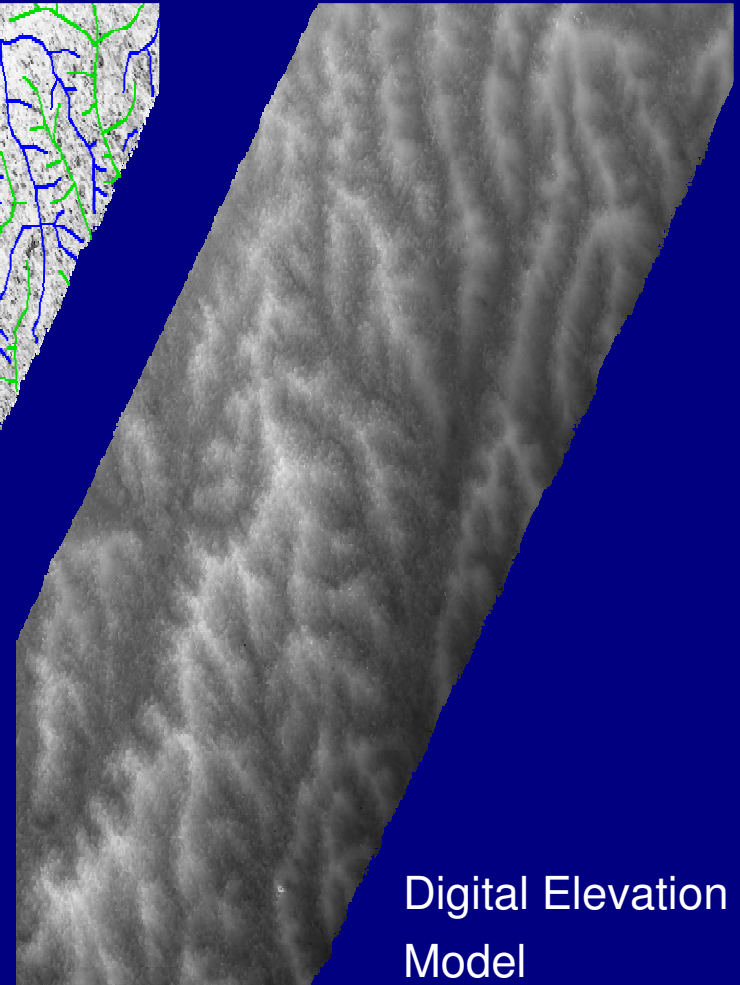
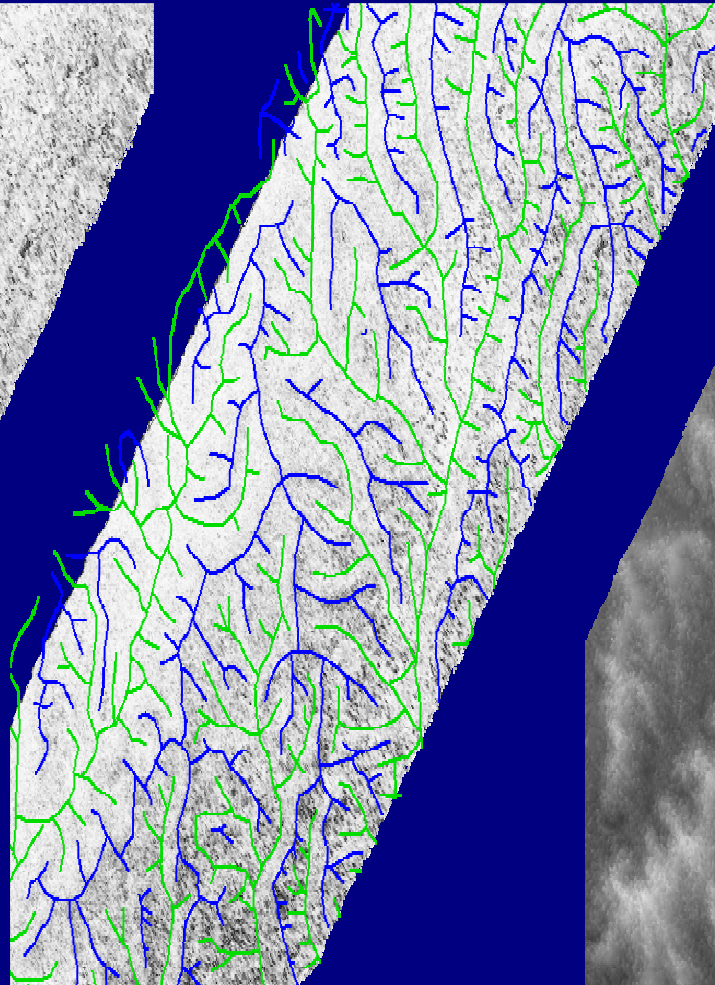
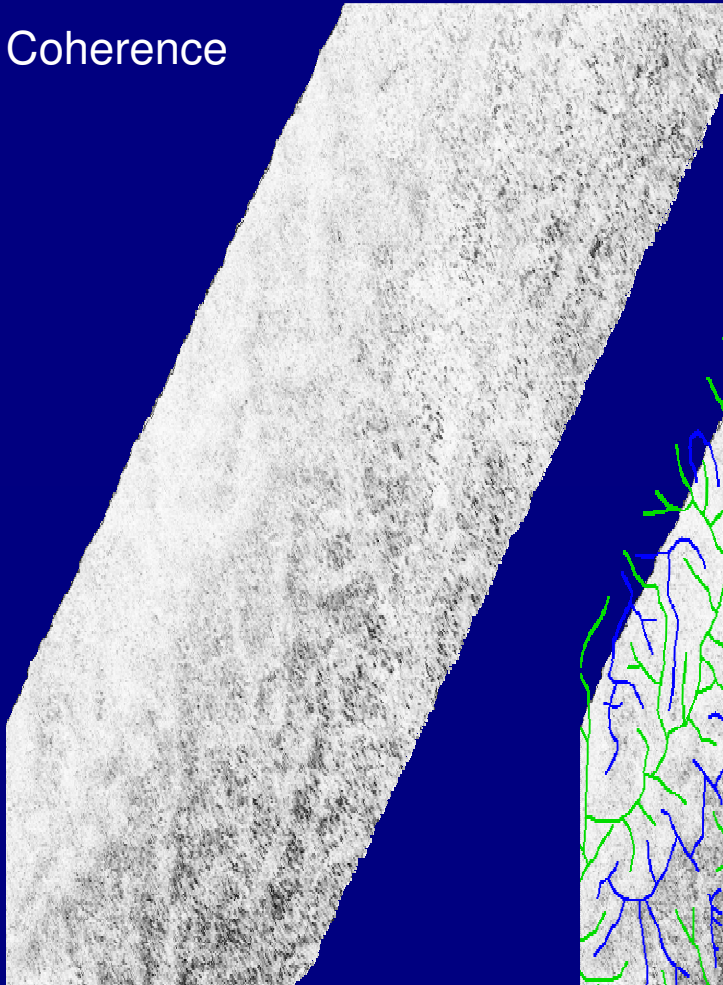
Deutsches Zentrum  
für Luft- und Raumfahrt e.V.  
in der Helmholtz-Gemeinschaft

Microwaves and Radar Institute / Pol - InSAR Research Group



# Topographic Dependency of InSAR Coherence (P band)

Coherence



Digital Elevation  
Model

Topo Lines over Coherence: ridge (blue), valley (green)

# The Effect of Topography on InSAR Coherence

Interferometric  
Coherence:

$$\tilde{\gamma}(\vec{w}) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m(\vec{w})}{1 + m(\vec{w})}$$

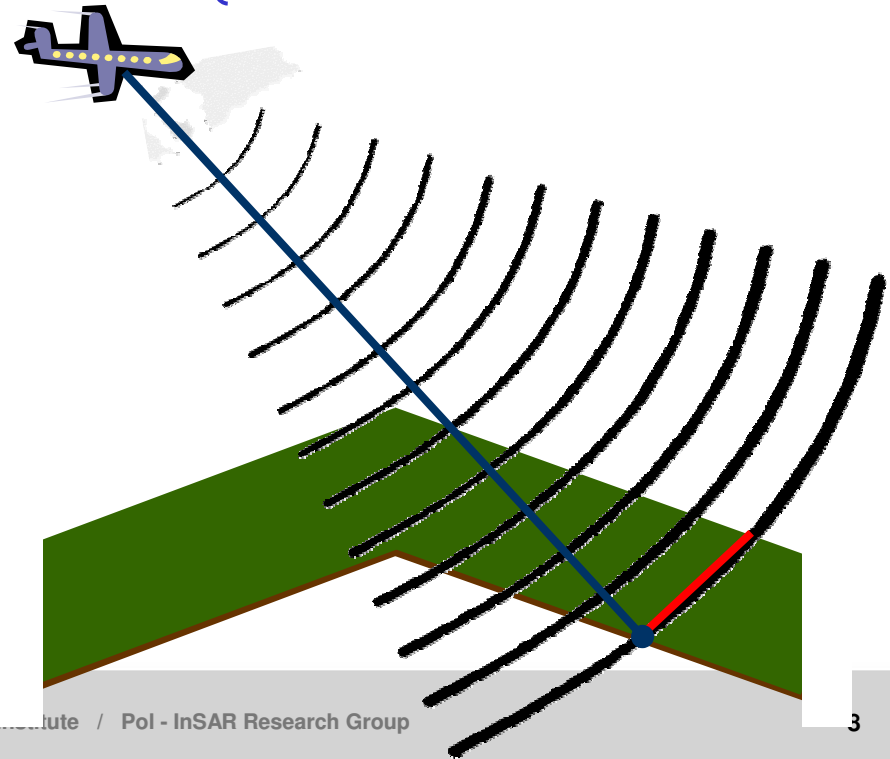
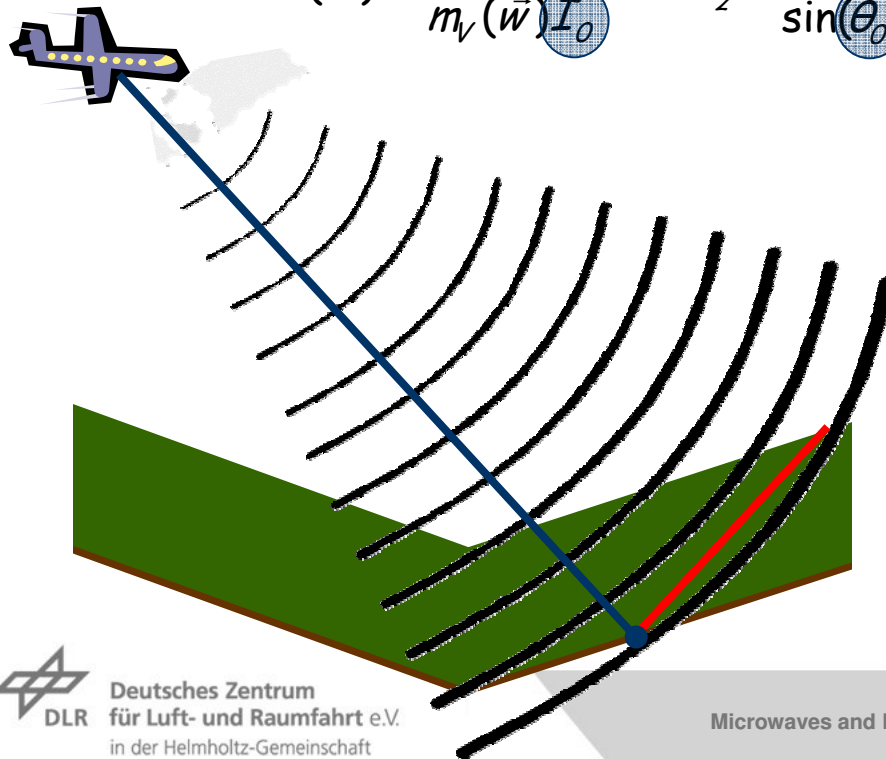
Volume  
Coherence:

$$\tilde{\gamma}_V = \frac{I}{I_0}$$

$$\begin{cases} I = \int_0^{h_V} \exp(i\kappa_z z') \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz' \\ I_0 = \int_0^{h_V} \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz' \end{cases}$$

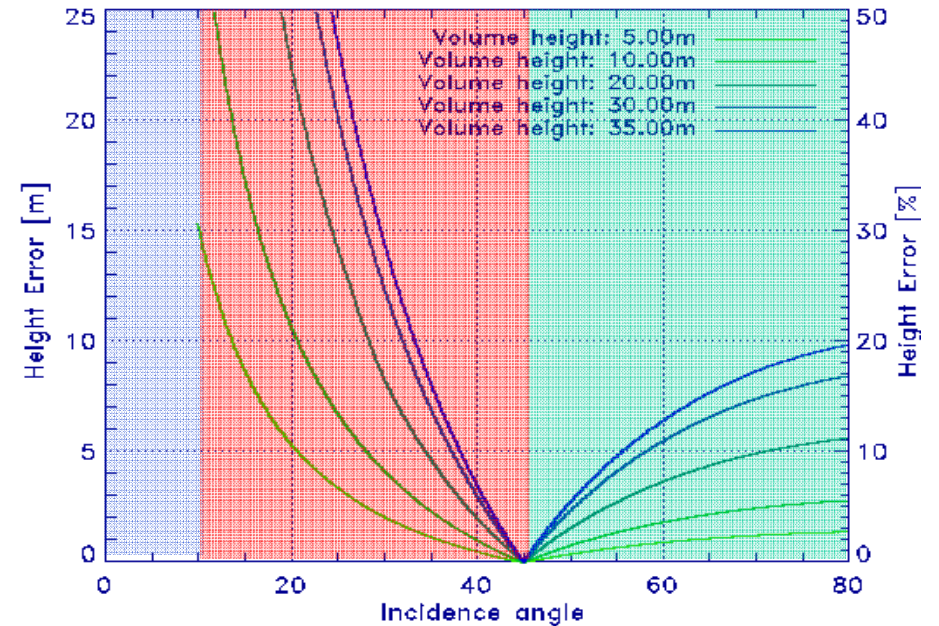
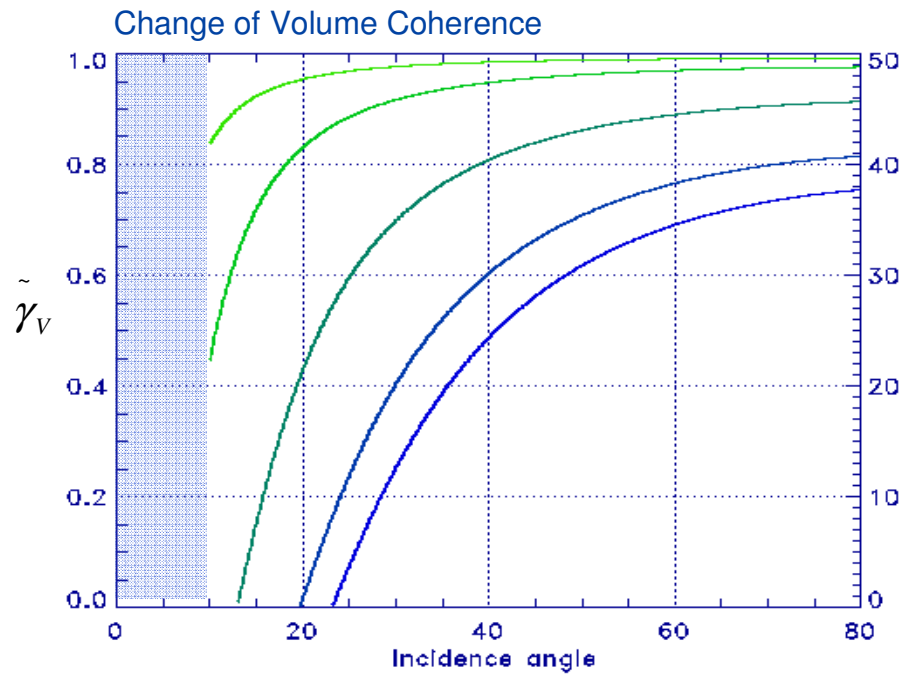
$$m(\vec{w}) = \frac{m_G(\vec{w})}{m_V(\vec{w}) I_0}$$

$$\kappa_z = \frac{\kappa \Delta\theta}{\sin(\theta_0)}$$





# Topography Induced Height Error



Modelling Parameters:

Extinction: 0dB/m

Incidence angle: 45°

Vertical Wavenumber: 0.1

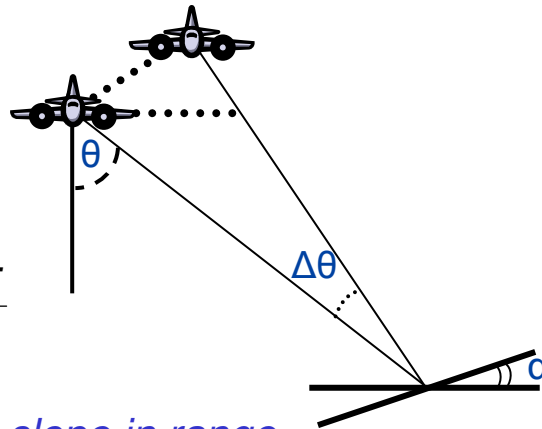
# Terrain Compensation: Vertical Wavenumber

Terrain Adaptive  
Vertical Wave-Number:

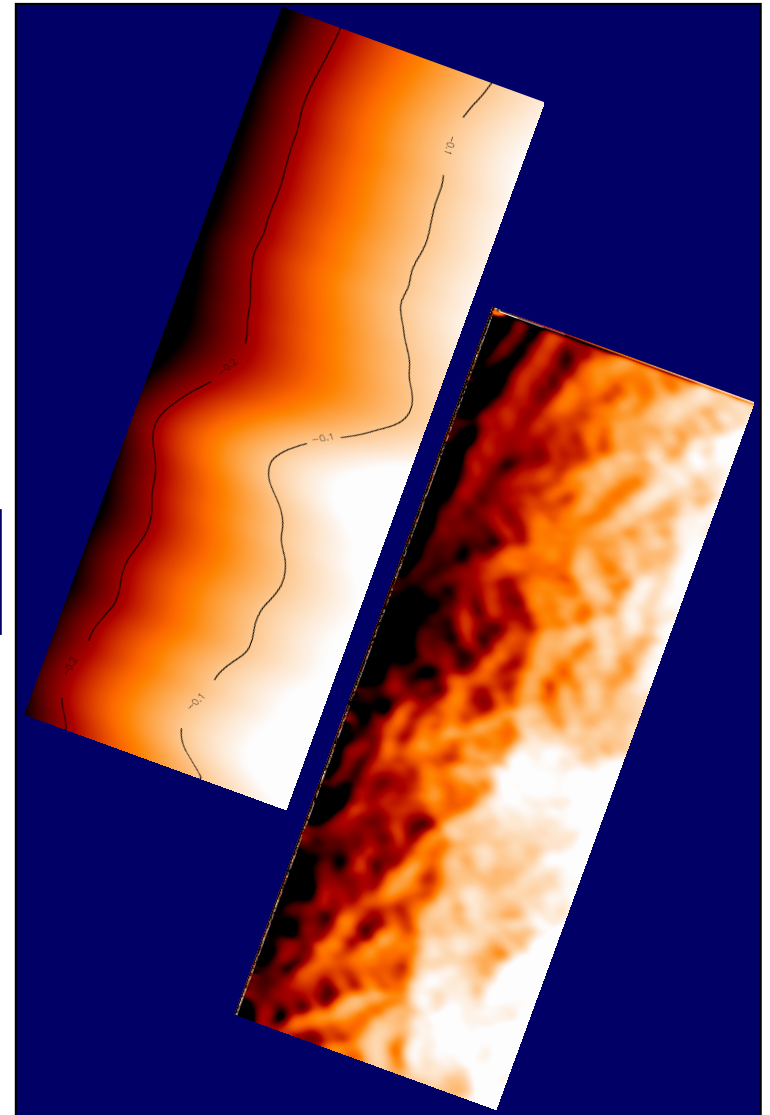
$$k_z = \frac{k\Delta\theta}{\sin(\theta - \alpha)}$$

$$k = \frac{4\pi}{\lambda}$$

where  $\alpha$  is the terrain slope in range.



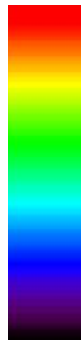
$\alpha$  is estimated from the low-pass filtered X-band DEM  
(to filter-out the DEM variation due to vegetation).





# Validation Sungai Wain Plot

Forest Height [m]



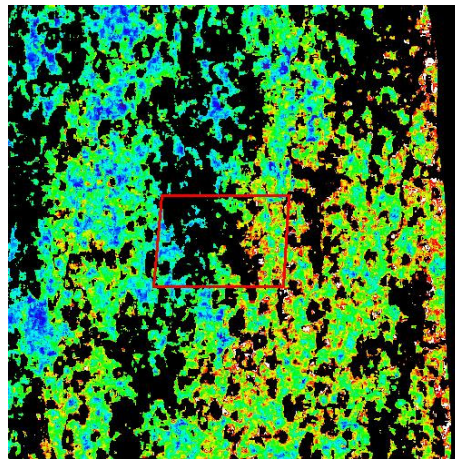
50m

37m

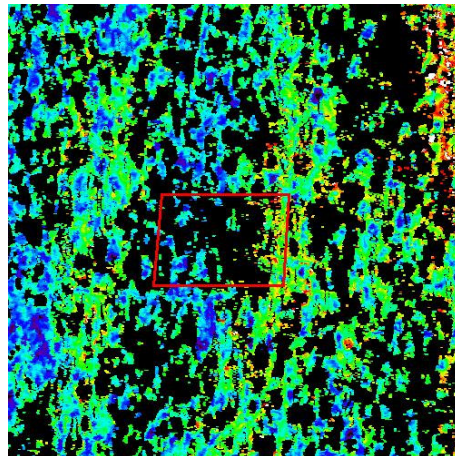
25m

12m

0m

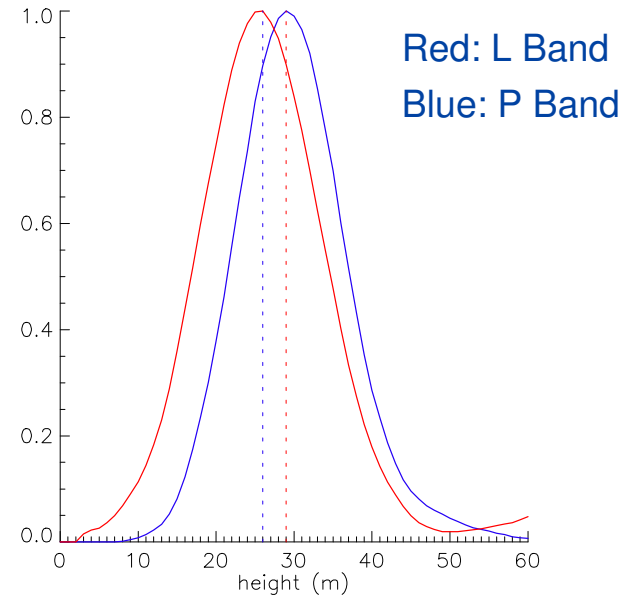


P – Band



L – Band

Radar Heights



Reference Height  
from Ground

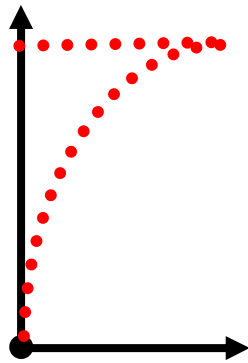
Measurements: 27m

L Band Mean: 26m  
P Band Mean: 29m



Deutsches Zentrum  
für Luft- und Raumfahrt e.V.  
in der Helmholtz-Gemeinschaft

# RVoG Inversion at X-band



$$\tilde{\gamma}_1(\vec{w}_1) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m_1(\vec{w}_1)}{1 + m_1(\vec{w}_1)}$$

$$\tilde{\gamma}_2(\vec{w}_2) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m_2(\vec{w}_2)}{1 + m_2(\vec{w}_2)}$$

$$\tilde{\gamma}_3(\vec{w}_3) = \exp(i\phi_0) \frac{\tilde{\gamma}_V + m_3(\vec{w}_3)}{1 + m_3(\vec{w}_3)}$$

*Assumption:*

$$m_1(\vec{w}_1) = m_2(\vec{w}_2) = m_3(\vec{w}_3) = 0$$



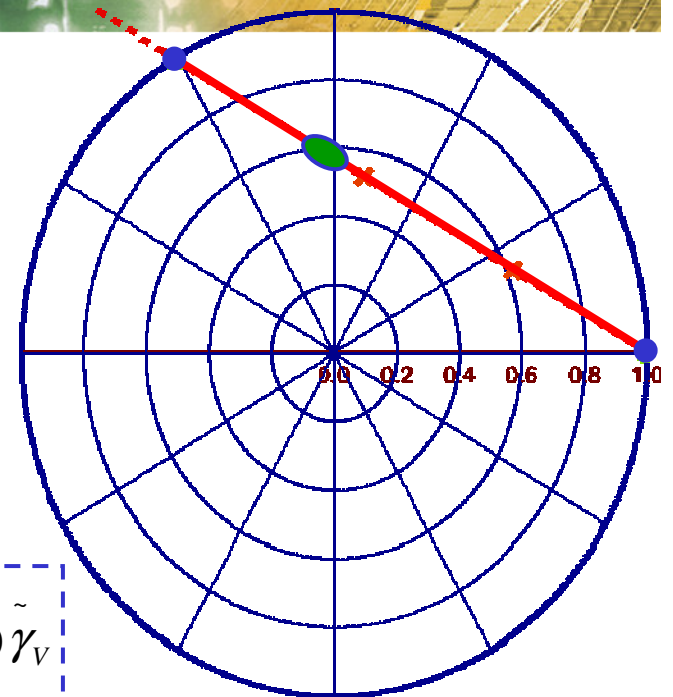
$$\tilde{\gamma}_1(\vec{w}_1) \approx \tilde{\gamma}_2(\vec{w}_2) \approx \tilde{\gamma}_3(\vec{w}_3) \approx \exp(i\phi_0) \tilde{\gamma}_V$$

$$\tilde{\gamma}_V(h_V, \sigma | \kappa_z) = \frac{I}{I_0} \left\{ \begin{array}{l} I = \int_0^{h_V} \exp(i\kappa_z z') \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz' \\ I_0 = \int_0^{h_V} \exp\left(\frac{2\sigma z'}{\cos\theta_0}\right) dz' \end{array} \right.$$



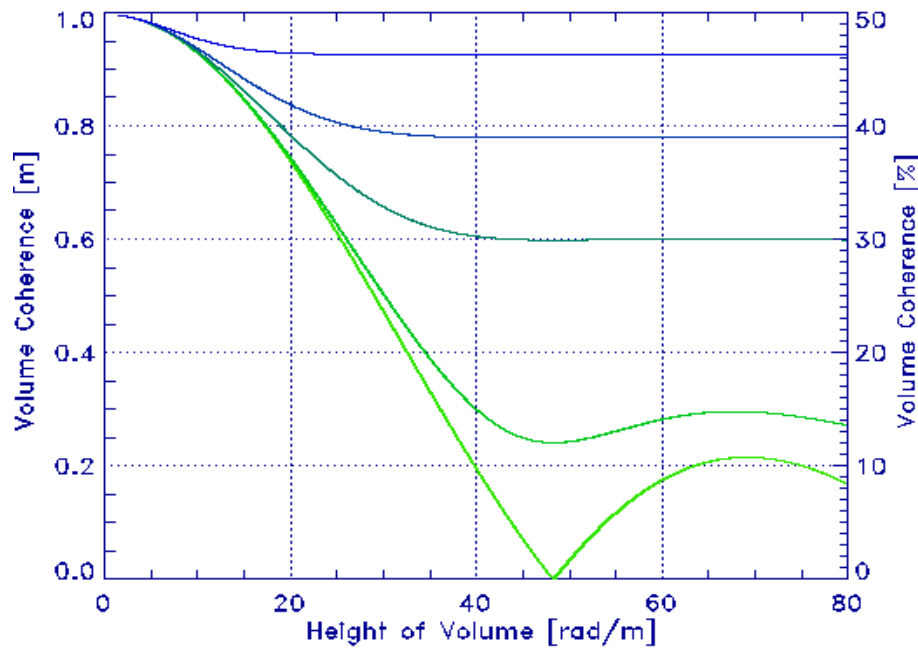
$$|\tilde{\gamma}_i(\vec{w}_i)| = |\tilde{\gamma}_V(h_V, \sigma | \kappa_z)|$$

*Underdetermined:  
1 Equation for 2 Unknowns*

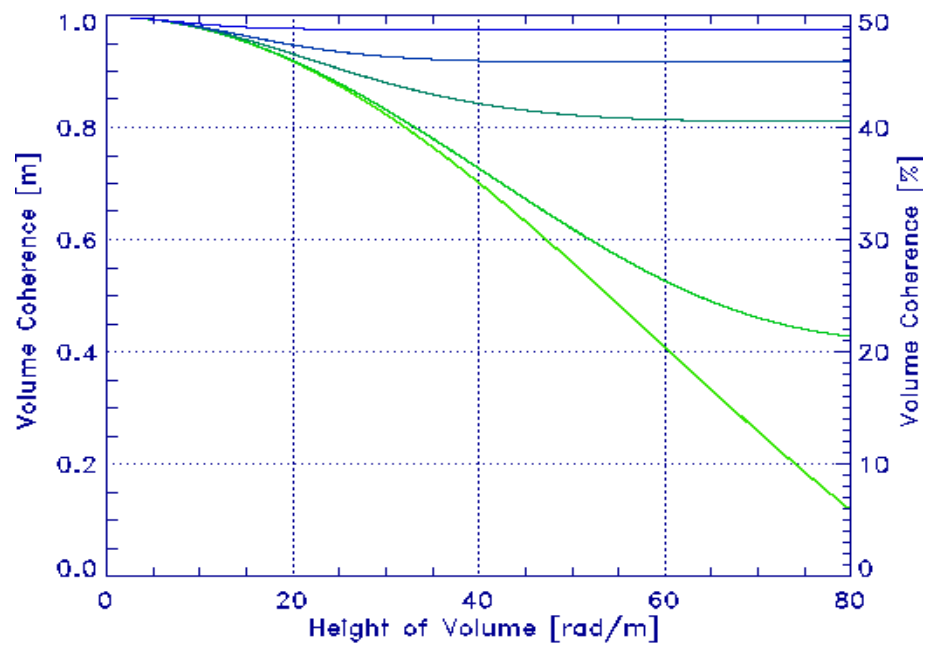




# Performance of X-band Inversion for DLR E-SAR



Vertical Wavenumber: 0.13



Vertical Wavenumber: 0.07

Extinction:

- 0 dB/m
- 0.1 dB/m
- 0.3 dB/m
- 0.5 dB/m
- 1.0 dB/m

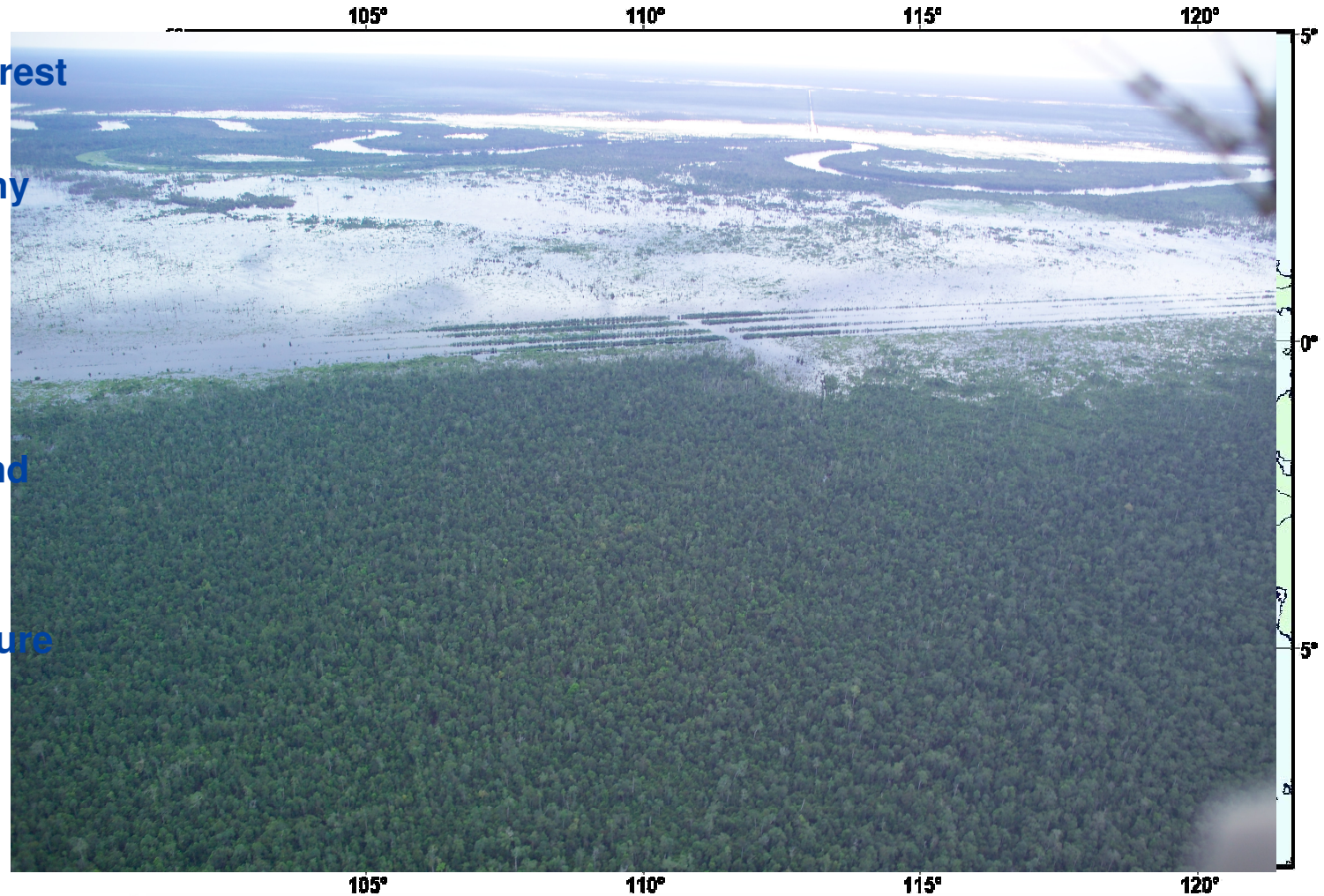


Deutsches Zentrum  
für Luft- und Raumfahrt e.V.  
in der Helmholtz-Gemeinschaft

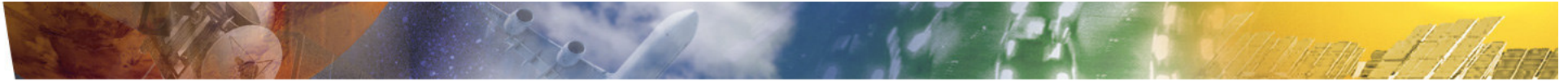
Microwaves and Radar Institute / Pol - InSAR Research Group

## Test Site: Mawas

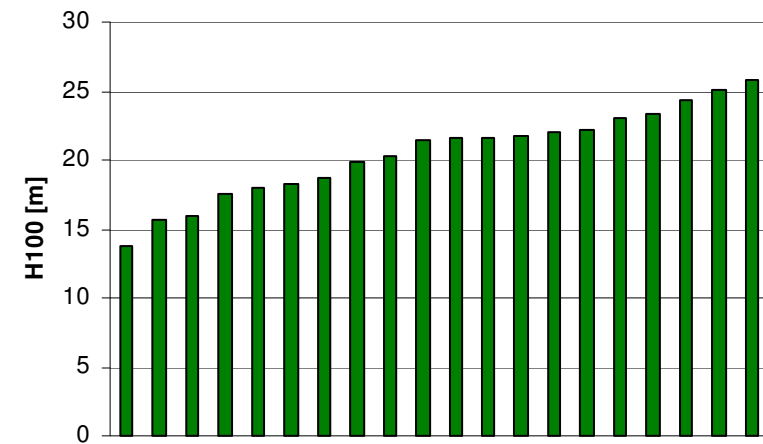
- Peat swamp forest
- Flat Topography
- Forest Height:  
15m – 25m
- Biomass around  
100t/ha
- Uniform structure
- Open canopy







## Reference Height Mawas



21m

23m

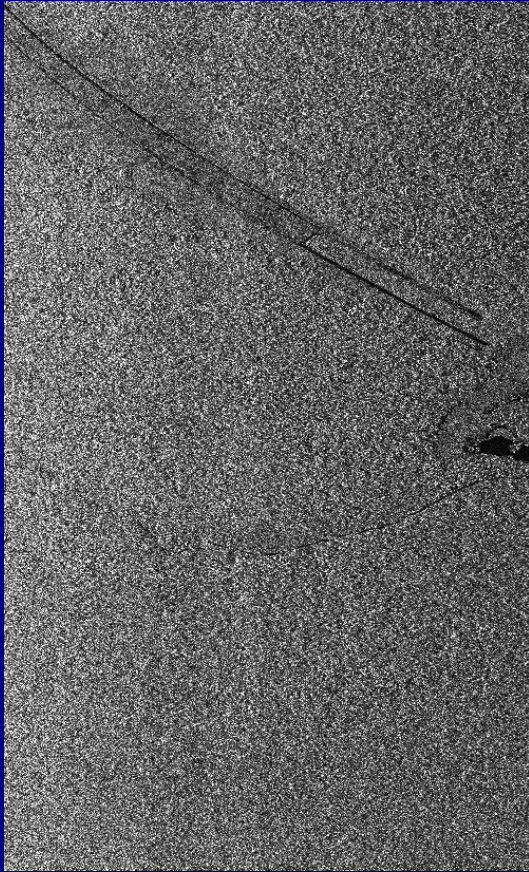
1
2
3
4
5
6
7
8
9
10

1
2
3
4
5
6
7
8
9
10

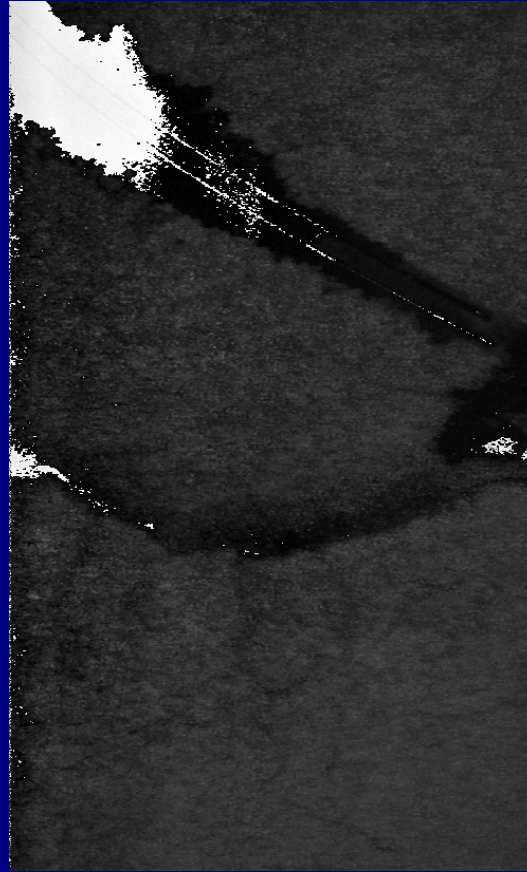
Plot design of  
Ground truth:  
20 squares of  
10m x 10m in  
two Transects



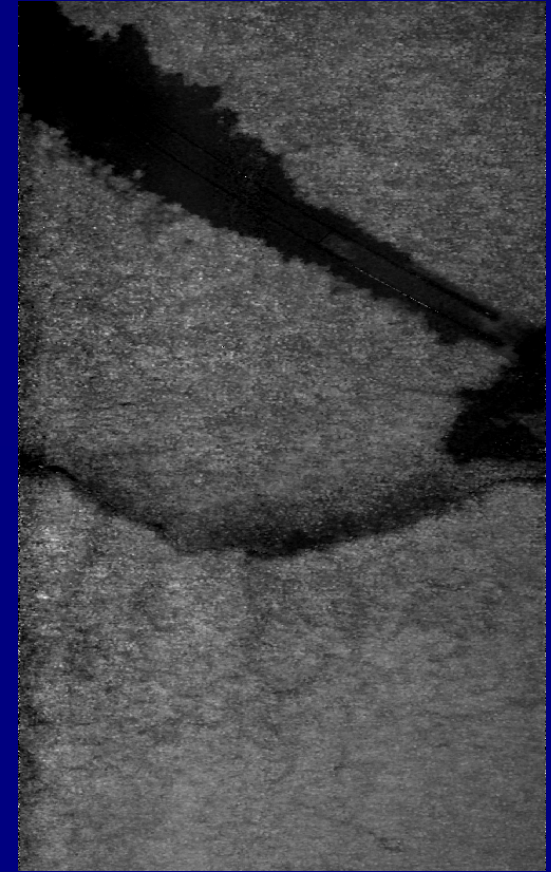
## Radar data Mawas X Band



Amplitude



Phase:  $-\pi$  to  $\pi$

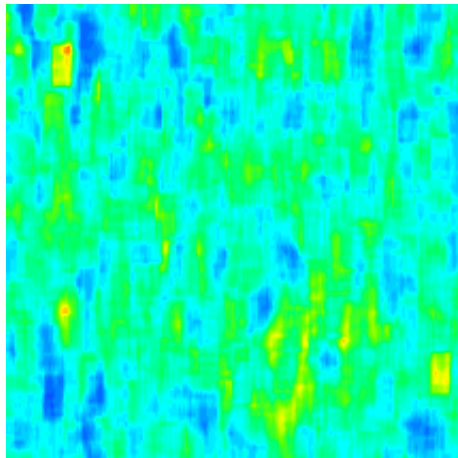


Phase difference: 0 to  $\pi$

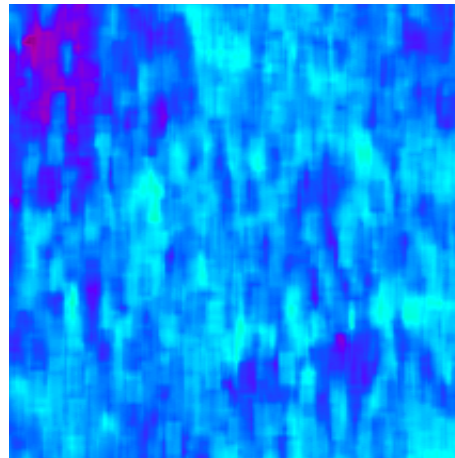




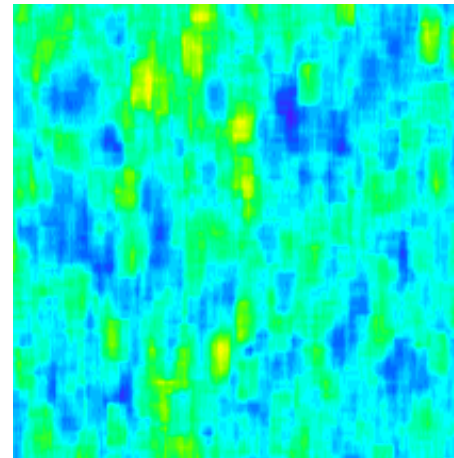
# Comparison Phase Center Height vs. Volume Height



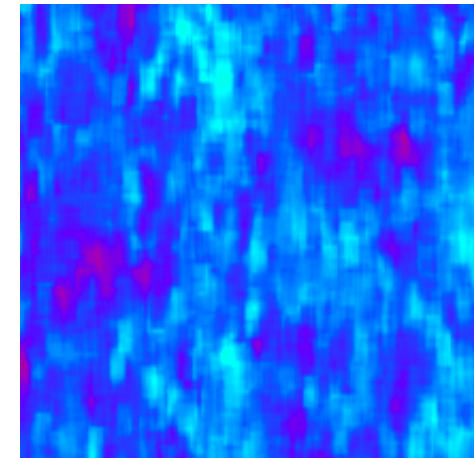
Coherence Height left



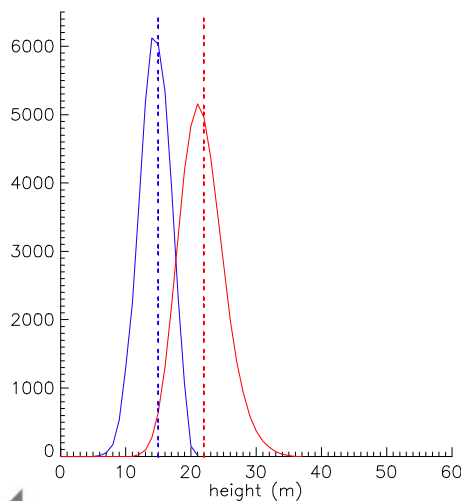
Phase Height left



Coherence Height right



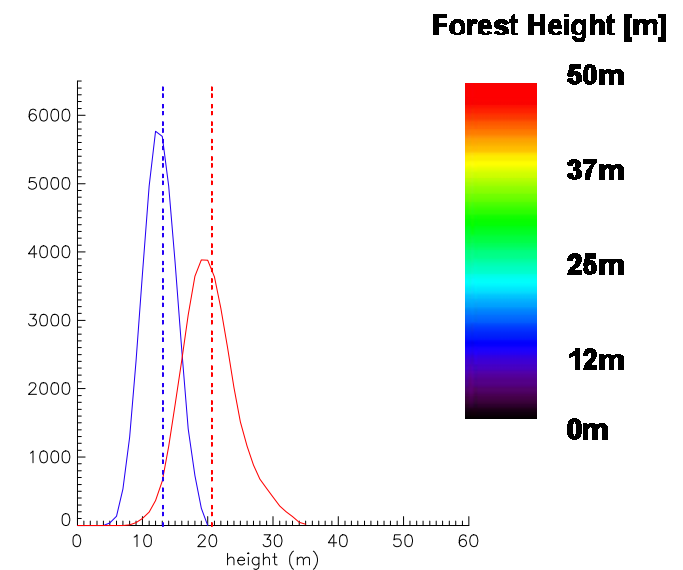
Phase Height right



Extinction: 0.1 db/m

Blue: Phase Height  
Red: Coherence Height

Ground measurements:  
21m – 23m





## Summary

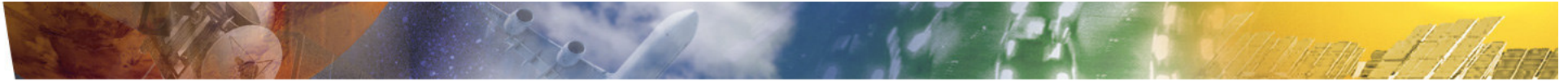
*Forest height over tropical rainforest was estimated and successfully validated in L band as well as in P band*

*Topography effects forest height estimation and has to be compensated*

*Forest height estimation using X band is possible for certain (sparse) forest conditions ( such as the mawas peat swamp forests)*

*X band Phase Scattering Center is lower than Pol-InSAR forest height*





***Thank you!***